

Ex: $\int_0^{\infty} \frac{1 + \cos^2(x)}{\sqrt{x}(2 - \sin^4(3x))} dx$ Looks like this'll diverge. Let's find then a smaller function that will diverge.

Let's find it: $\frac{1 + \cos^2(x)}{\sqrt{x}(2 - \sin^4(3x))}$ \rightarrow we know: $0 \leq \cos^2(x) \leq 1$, then

$$\geq \frac{1}{\sqrt{x}(2 - \sin^4(3x))} \quad \left. \begin{array}{l} \\ \end{array} \right\} 0 \leq \sin^4(3x) \leq 1$$

$$\geq \frac{1}{\sqrt{x}(2)} = \frac{1}{2} \cdot \frac{1}{x^{1/2}}$$

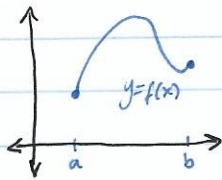
We know $\frac{1}{2} \int_0^{\infty} \frac{1}{x^{1/2}} dx$ diverges since $\frac{1}{2} \leq 1$.

Therefore by comparison test, the original integral diverges.

Things about 1st exam:

- \rightarrow "Here's a bunch of integrals, do them".
- \rightarrow Integration by parts, fundamental.
- \rightarrow Trig. integrals.
- \rightarrow Trig. substitutions
- \rightarrow Partial Fractions (integral).
- \rightarrow Improper Integrals
- \rightarrow Comparison Test

ARC LENGTH:



What's the length of this curve?

So, given a curve by $y=f(x)$, The arclength is calculated by:

$$L = \int_a^b \sqrt{1 + [f'(x)]^2} dx = \int_a^b \sqrt{1 + [dy/dx]^2} dx \quad y=f(x), a \leq x \leq b$$

$$L = \int_c^d \sqrt{1 + [g'(y)]^2} dy = \int_c^d \sqrt{1 + [dx/dy]^2} dy \quad x=g(y), c \leq y \leq d$$

→ Another way of writing the arclength formula is:

$$L = \int ds$$

where ds can be something different depending on how the curve is given.

$$ds = \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx \quad \text{if } y = f(x), \quad a \leq x \leq b$$

or

$$ds = \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy \quad \text{if } x = g(y), \quad c \leq y \leq d$$