

April 16, 2019

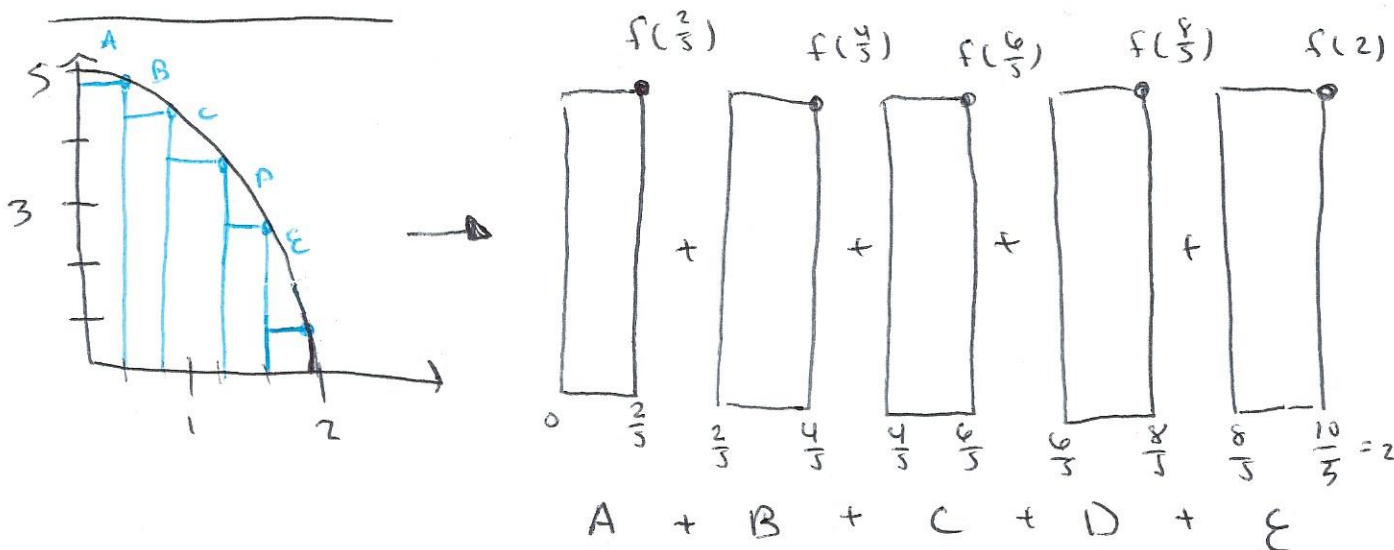
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$$A = \frac{2}{3} \sum_{i=1}^5 f(x_i), \quad x_i = a + \Delta x(i-1)$$

$$= \frac{2}{3} \left(5 + \frac{121}{25} + \frac{109}{25} + \frac{89}{25} + \frac{61}{25} \right) = \frac{202}{25}$$

for left endpoints, area is $\frac{202}{25} = 8.08$

Right endpoints



Calculate areas

$$\begin{aligned} A &= A_A + A_B + A_C + A_D + A_E \\ &= \left(\frac{2}{5}\right) f\left(\frac{2}{5}\right) + \left(\frac{2}{5}\right) f\left(\frac{4}{5}\right) + \left(\frac{2}{5}\right) f\left(\frac{6}{5}\right) + \left(\frac{2}{5}\right) f\left(\frac{8}{5}\right) + \left(\frac{2}{5}\right) f(2) \\ &= \frac{2}{5} \left(f\left(\frac{2}{5}\right) + f\left(\frac{4}{5}\right) + f\left(\frac{6}{5}\right) + f\left(\frac{8}{5}\right) + f(2) \right) \\ &= \frac{2}{5} \sum_{i=1}^5 f(x_i), \quad \text{where } x_i = a + \Delta x(i-1) \\ &= \frac{2}{5} \left(\frac{121}{25} + \frac{109}{25} + \frac{89}{25} + \frac{61}{25} + 1 \right) = \frac{162}{25} \end{aligned}$$

for right endpoints, area is $\frac{162}{25} = 6.48$

The average of left+right endpoints is

$$\left(\frac{\frac{202}{25} + \frac{162}{25}}{2} \right) = \frac{182}{25} = \boxed{7.28}$$