

" matrices and linear system

" vector spaces

" linear transformation

\* A linear equation, in  $n$  variables  $x_1, x_2, \dots, x_n$

is of the form

$$a_1x_1 + a_2x_2 + \dots + a_nx_n = b$$

$a_1, a_2, \dots, a_n, b$  are constants and  $a_1, a_2, \dots, a_n$  are

not all zero.

Example:

2  
variable

$$\left. \begin{aligned} 3x + 2y &= 1 \\ ax + by &= c \end{aligned} \right\}$$

equation of a line

3  
variable

$$x + 2y - 3z = 5 \rightarrow$$

equation of plane

more  
variables

$$2x_1 + 3x_2 - x_3 + x_4 = 2 \rightarrow \text{eq. of a 4-D hyper-plane}$$

non-example:

23-01-2019

2

→ NO power of variables

→ NO multiplying variable together.

→ variable cannot be argument of trig, log, exp

linear:  $2x + \ln(3)y = 2$

non linear:  $2x + 3 \ln(y) = 2$

$$2xy + 3y = 6$$

$$2x^2 + 3y = 7$$

A soln to a linear equation is a sequence of  
number  $t_1, \dots, t_n$  such that

$$a_1 t_1 + a_2 t_2 + \dots + a_n t_n = b \text{ in a true}$$

statement.

The set of all soln of a linear eq. is called the  
solution set.

Example:

$$3x + 2y = 1$$

let  $x = t$ , where  $t \in \mathbb{R}$

$$y = -\frac{3}{2}x + \frac{1}{2}$$

$$\text{soln set: } \left\{ y \mid y = \frac{-3}{2}t + \frac{1}{2}, t \in \mathbb{R} \right\}$$

$$x = -\frac{2}{3}y + \frac{1}{3} \quad \left\{ \begin{array}{l} x \\ x \end{array} \right. = \frac{-2}{3} S + \frac{1}{3} \left. \right\}$$

3

23-01-2019