

Date - 4.18.19
Ms. Aguiñe
Math 1342-13

8.2: Distribution of the sample proportion:

∴ sample proportion, \hat{p} , is given

$$\text{by } \hat{p} = \frac{x}{n}.$$

p = proportion of population that plans to work on vacation.

$n = 1200$ Adult Americans

552 planned to work on vacation.

$$\hat{p} = \frac{x}{n} = \frac{552}{1200} = 0.46$$

about 46% of population plans to work on vacation.

* sampling distribution of \hat{p} .

$$* np(1-p) \geq 10.$$

$$* \mu_{\hat{p}} = p$$

$$* \sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$$

Exercise 30

$$p = 0.76$$

$$n = 60$$

\hat{p} = describe

60 is less than 5% of the population of Adult Americans.

ii samples are independent.

is \hat{p} approximately normal?

$$np(1-p) \geq 10$$

$$(60)(0.76)(0.24) \geq 10$$

$$10.994 \geq 10$$

↳ is normal.

$$\mu_{\hat{p}} = p = 0.76$$

$$\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}} = \sqrt{\frac{(0.76)(0.24)}{60}} = 0.055$$

ex4

$$p = 15\% = 0.15$$

(a) $n = 120$

$$P(\hat{p} \leq 0.12)$$

$$np(1-p) \geq 10$$

$$(120)(0.15)(0.85) \geq 10$$

$$15.3 \geq 10$$



if \hat{p} is approximately normal, we use z-scores and standard normal table.

$$\mu_{\hat{p}} = p = 0.15$$

$$\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}} = \sqrt{\frac{(0.15)(0.85)}{120}} \approx \boxed{0.033}$$

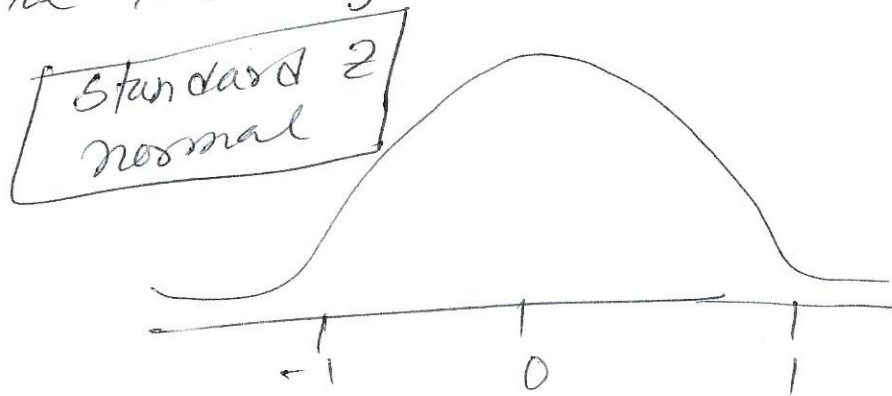
$$z = \frac{x - \mu}{\sigma}$$

$$z = \frac{\hat{p} - np^{\wedge}}{\sigma_{\hat{p}}}$$

$$z = \frac{(0.12) - (0.15)}{0.033}$$

$$z = -0.91$$

from table V, area under curve to the left of $z = -0.91$ is 0.1814



probability that \hat{p} is no more than 12% 0.1814 or 18.14%

(b) $n = 120$
 $x = 26$ have hearing trouble after
listening to headphones.

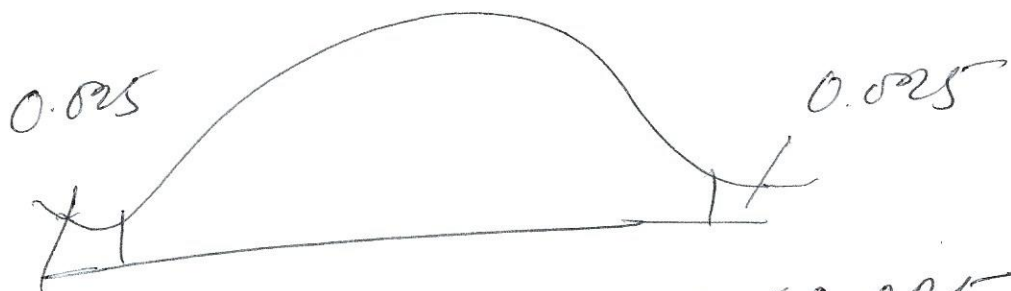
What can we conclude?

$$p = 0.15$$

$$\hat{p} = \frac{26}{120} = \frac{x}{n} = 0.217$$

$$z = \frac{\hat{p} - p}{\sqrt{p(1-p)}} \quad z = \frac{0.217 - 0.15}{\sqrt{0.15(0.85)}}$$

$$z = 2.06$$



$$0.0197 < 0.025$$

unusual result for
hearing loss.