

• NEGATIVE INTEGER EXPONENT

◦ show: $2^{-3} = \frac{1}{2^3}$

proof: we know $2^3 = 8$

and $2^3 \cdot 2^{-3} = 2^{(3+(-3))} = 2^0 = 1$

$$\begin{array}{c} \downarrow \quad \downarrow \\ 8 \cdot \frac{1}{8} = 1 \end{array}$$

multiplying fractions: $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$

$\frac{8}{1} \cdot \frac{1}{8} = \frac{8}{8} = 1$

$$2^3 = 2 \cdot 2 \cdot 2 = 8$$

$$2^0 = 1$$

• definition: RECIPROCAL

Two numbers whose product is 1

e.g. -2 and $-\frac{1}{2}$

$\frac{3}{5}$ and $\frac{5}{3}$

$\cdot 7 = \frac{7}{10}; \frac{10}{7}$

$\cdot 41 = \frac{41}{100}; \frac{100}{41}$

→ change a fraction upside down to get its reciprocal.

• calculation: $\boxed{\frac{1}{x}}$ or $\boxed{x^{-1}}$

✱ RECIPROCAL OF ZERO IS NOT DEFINED!

since anything multiplied by zero is still zero, in other words, nothing multiplied by zero will turn out to be 1.

• Rules:

◦ (1). Any number to a negative power is the same as its reciprocal to the positive power

$$2^{-3} = \left(\frac{1}{2}\right)^3 = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1 \cdot 1 \cdot 1}{2 \cdot 2 \cdot 2} = \frac{1^3}{2^3} = \frac{1}{8}$$

$$\left(\frac{2}{3}\right)^2 = \left(\frac{3}{2}\right)^2 = \left(\frac{3}{2}\right) \cdot \left(\frac{3}{2}\right) = \frac{3 \cdot 3}{2 \cdot 2} = \frac{9}{4}$$

(2). I am free to move any factor to the other part of the fraction -
IF I change the sign of the exponent.

$$2^{-3} = \frac{2^{-3}}{1} = \frac{1}{2^3} = \frac{1}{8}$$

$$5ab^{-2} = \frac{5ab^{-2}}{1} = \frac{5a}{b^2}$$

$$\frac{1}{6a^{-5}} = \frac{a^5}{6}$$

WEBASSIGN

$$(1) 3^{-1} + 4^{-1} = \frac{3^{-1}}{1} + \frac{4^{-1}}{1} = \frac{1}{3} + \frac{1}{4} = \frac{1}{3} + \frac{1}{4} = \frac{1 \cdot 4 + 1 \cdot 3}{(3)(4)} = \frac{7}{12} = \boxed{7/12}$$

★ TO EVALUATE ADDITION/SUBTRACTION OF TWO FRACTIONS

(1). multiply the denominator

(2) start with upper left and cross multiply.

} "HANDY-DANDY" METHOD

$$\frac{4}{9} - \frac{3}{7} = \frac{4 \cdot 7 - 3 \cdot 9}{9 \cdot 7} = \frac{28 - 27}{63} = \frac{1}{63}$$

$$\frac{3}{x} + \frac{5}{y} = \frac{3y + 5x}{xy}$$

$$(2) (3^{-1})^{-2} = 3^{(-1) \cdot (-2)} = 3^2 = 9$$

$$\hookrightarrow = \left(\frac{1}{3}\right)^{-2} = 3^2 = 9$$

Third Property of Exponent.

$$\frac{x^5}{x^3} = x^{5-3} = x^2$$

$$(3) \frac{3x^6}{x^5} = \frac{3x^{6-5}}{1} = \frac{3x^1}{1} = 3x ; \frac{25a^3b^7}{40a^{10}b^2} = \frac{5b^{7-2}}{8a^{10-3}} = \frac{5b^5}{8a^7}$$