

Pg 249

19) $c(x) = -2x^2 - 10x + 4$

a) write in vertex form $(a(x-h)^2 + k)$

$$= -2\left(x^2 + 5x + \frac{25}{4}\right) + 4 + \frac{25}{2}$$

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Complete the Square

$$\begin{aligned} 5 \div 2 &= \frac{5}{2} \\ \left(\frac{5}{2}\right)^2 &= \left(\frac{5}{2}\right)\left(\frac{5}{2}\right) = \frac{25}{4} \end{aligned}$$

$$-2 \cdot \frac{25}{4}$$

$= -\frac{25}{2}$, so add $\frac{25}{2}$ to cancel out.

$$c(x) = -2\left(x + \frac{5}{2}\right)^2 + \frac{33}{2}$$

b) Vertex: $\left(\frac{-5}{2}, \frac{33}{2}\right)$

c) x-ints: (x-intercepts)

Set $c(x) = 0$, then

$$0 = -2\left(x + \frac{5}{2}\right)^2 + \frac{33}{2}$$

$$-\frac{33}{2} = -2\left(x + \frac{5}{2}\right)^2$$

$$\frac{33}{4} = \left(x + \frac{5}{2}\right)^2$$

$$\pm \frac{\sqrt{33}}{2} = x + \frac{5}{2}$$

$$x = \frac{-5 \pm \sqrt{33}}{2}$$

$$\left(\frac{-5 + \sqrt{33}}{2}, 0\right) \quad \& \quad \left(\frac{-5 - \sqrt{33}}{2}, 0\right)$$

(finite)

g) Max or min value of

$c(x)$; max of $c(x) = \frac{33}{2}$

d) y-ints:

Set all $x = 0$, Set $c(x) = y$,

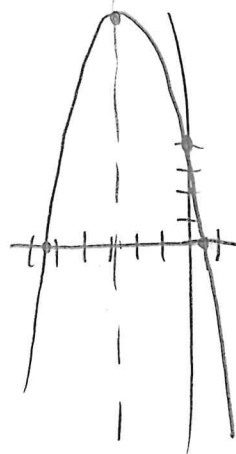
$$y = -2(0^2) - 10(0) + 4$$

$$y = 4$$

$$(0, 4)$$

★ You can use either original equation or the vertex version to find x & y intercepts.

e) Sketch $c(x)$



f) Line of symmetry

$$@ x = \frac{-5}{2}$$

h) D: $(-\infty, \infty)$

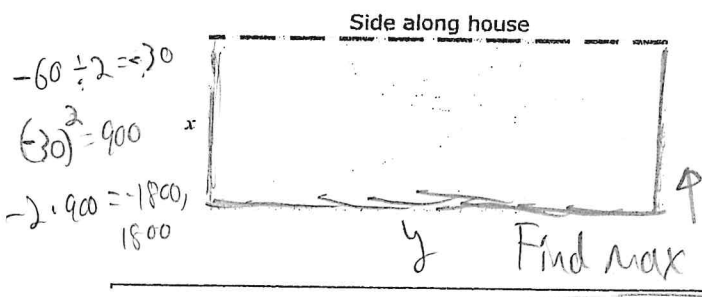
R: $(-\infty, \frac{33}{2}]$

ALEKS work

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Sam has 120 meters of fencing. He will use it to form three sides of a rectangular garden. The fourth side will be along a house and will not need fencing. Find max area.

As shown below, one of the sides has length x (in meters).



$$P = 2x + y$$

$$120 = 2x + y$$

$$y = -2x + 120$$

$$A = xy$$

$$A = x(-2x + 120)$$

$$A = -2x^2 + 120x$$

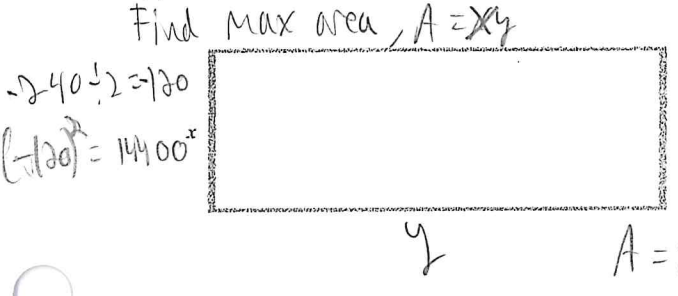
$$A = -2(x^2 - 60x + 900) + 1800$$

$$A = -2(x - 30)^2 + 1800$$

vertex: $(30, 1800)$

If $x = 30$, $120 = 2(30) + y$, $y = 60$, $A = 30 \cdot 60 = 1800 \text{ m}^2$

A school wishes to enclose its rectangular playground using 480 meters of fencing. Suppose that a side length (in meters) of the playground is x , as shown below.



$$P = 2x + 2y$$

$$480 = 2x + 2y$$

$$2y = 480 - 2x$$

$$y = 240 - x$$

$$A = xy \rightarrow A = x(240 - x)$$

$$A = -x^2 + 240x$$

$$A = -1(x^2 - 240x + 14400) + 14400$$

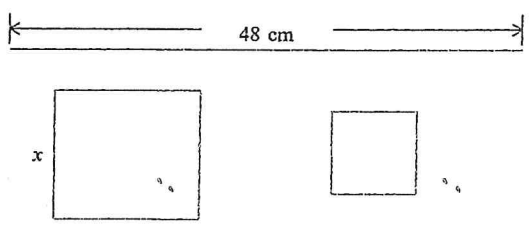
$$A = -1(x - 120)^2 + 14400$$

vertex: $(120, 14400)$

If $x = 120$, $y = 240 - x = 240 - 120 = 120$

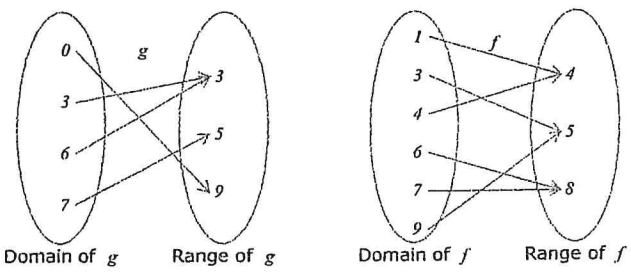
$$A = xy = (120)(120) = 14400 \text{ m}^2$$

A wire that is 48 centimeters long is shown below. The wire is cut into two pieces, and each piece is bent and formed into the shape of a square.



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Two functions g and f are defined in the figure below.



Find the domain and range of the composition $f \circ g$. Write your answers in set notation.