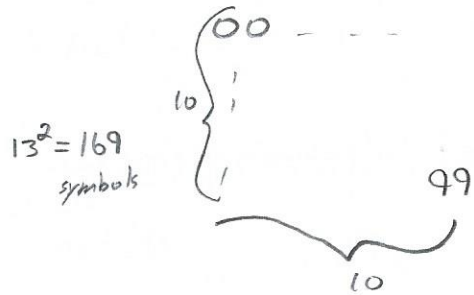
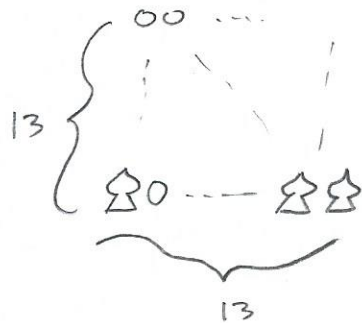


$$\diamond 5 \spadesuit = \diamond 00 + 50 + \spadesuit$$



Hindu-Arabic	base 13
169	100
$11 \times 169 = 1859$	$\diamond 00$
$5 \times 13 = 65$	50
12	$\spadesuit$

$$\diamond 5 \spadesuit = \diamond 00 + 50 + \spadesuit = 1859 + 65 + 12 = \boxed{1936}$$

A good way to solve:

$$\begin{aligned} 572 &= 500 + 70 + 2 \\ &= 5 \times 10^2 + 7 \times 10^1 + 2 \times 10^0 \end{aligned}$$

$$\diamond 5 \spadesuit = \diamond \times 13^2 + 5 \times 13^1 + \spadesuit \times 13^0$$

## Ch. 2

Associative law of addition: For any whole numbers  $a, b, c$ ,  
 $(a+b)+c = a+(b+c)$

Commutative law of addition: For any whole numbers  $a, b$ ,  
 $a+b = b+a$

Associative law of multiplication: For any whole numbers  $a, b, c$ ,  
 $a(bc) = (ab)c$

Commutative law of multiplication: For any whole numbers  $a, b$ ,  
 $ab = ba$

Ex:

Skip count 2 rows in  
2 digit grid  
↓

$$\begin{aligned} 23+51 &= (20+3) + (50+1) \\ &\quad \downarrow \\ &\quad \text{skip 3 steps} \\ &= (50+20) + (3+1) && \Rightarrow \text{Using Associative law} \\ &= (70) + (4) \\ &\quad \downarrow \\ &\quad 7 \text{ rows} \\ &= \boxed{74} \end{aligned}$$

Ex:

Addition Algorithm:

$$\begin{array}{r} 23 = (20+3) \\ +51 = (50+1) \\ \hline 74 = 70+4 \end{array}$$

Ex.  $18 + 17 = (10+8) + (10+7)$   
 $= (10+10) + (8+7)$   
 $= 20 + 15$   
 $= 20 + (10+5)$   
 $= (20+10) + 5$   
 $= 30 + 5$   
 $= 35$

Ch. 2 Prob. 8

$$(x+y)(x+y) = xx + xy + yx + yy$$

⊛ We will need to use distributive law twice!

$$\overset{a}{(x+y)} (\overset{b}{x} + \overset{c}{y})$$

Distributive Law: For any whole numbers  $a, b, c$ ,

(i)  $a(b+c) = ab+ac$

(ii)  $(a+b)c = ac+bc$

$$(x+y)(x+y) = (x+y)x + (x+y)y \quad \text{by (i)}$$

$$= xx + yx + xy + yy \quad \text{by (ii)}$$

$$= xx + xy + yx + yy \quad \text{by Commutative}$$

$$xy + x^2 = x(y+x)$$

$$2x + 3x = (2+3)x$$

Prob.

Count with 0, 1, 2

$\begin{array}{r} \phantom{0} \overset{1}{2} 1 2 \\ + 1 0 2 \\ \hline 1 0 2 1 \end{array}$	<table style="border-collapse: collapse;"> <tr> <td style="padding-right: 10px;">00</td> <td style="padding-right: 10px;">01</td> <td>02</td> </tr> <tr> <td style="padding-right: 10px;">10</td> <td style="padding-right: 10px;">11</td> <td>12</td> </tr> <tr> <td style="padding-right: 10px;">20</td> <td style="padding-right: 10px;">21</td> <td>22</td> </tr> </table>	00	01	02	10	11	12	20	21	22
00	01	02								
10	11	12								
20	21	22								

Same thing as:

$$212 + 102 = (200 + 10 + 2) + (100 + 2)$$

$$= (200 + 100) + (10) + (2 + 2)$$

$$= 1000 + 10 + 11$$

$$= 1000 + (10 + 10) + 1$$

$$= 1000 + 20 + 1$$

$$\boxed{= 1021}$$