

Assigned HW: Ch. 1 - 1, 9

Ch. 2 - 1, 7, 8(i), (iii), 12

Ch. 4 - 5, 7, 8

Using 0, 1, 2, how many #'s come before 12121?

00 01 02

10 11 12

20 21 22

#'s before 10? 3

before 100? 9

before 1,000? 27

before 10,000? 81

000 ... 022

100 ... 122

200 ... 222

0000 0001 0002 0010 0011 0012 0020 0222
 1000 1222
 2000 2222

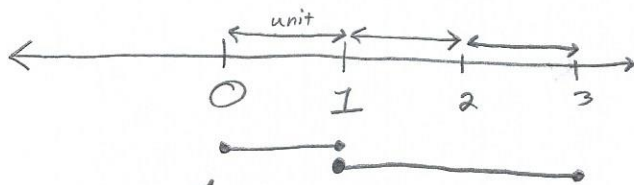
Hindu-Arabic	3 Fingered Alien	
81	10,000	10,000
$27 \cdot 2 = 54$	2000	12,000
9	100	12,100
6	20	12,120
1	1	12121

Total = 151 #'s before 12121

★ In problem explanations, assume your target audience has previous knowledge. Only go back 1 step in explanations.

Number Line:

We take for granted an infinite straight line.



This allows us to calculate steps and distance!

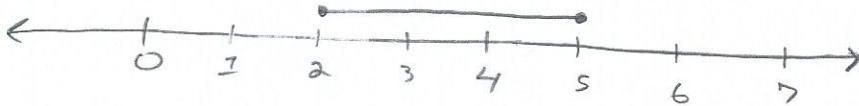
$$1+2$$

↳ 1 step, then 2 more steps.

↳ It's also the length of 3.

★ This helps show the equality of $1+2$ and $2+1$!

Lets use the notation $[2, 5]$ to denote the line segment with endpoints at 2 and 5.



Comparing Numbers:

Definition: Let a and b be whole numbers,

a is less than b if a comes before b in our method of counting.

We write $a < b$

Ex. Why is $45 < 123$?

$$45 = 045$$

So, in the three digit grid 045 is in the 1st row while 123 is in the next row.
Therefore, $045 < 123$.

Why is $56 < 70$?

In the 2 digit grid 56 is in the row that starts with 5's which comes before the row that starts with 7's (where 70 is located).

★ Test Questions: ★

Be prepared to explain your answers in terms of what has been covered in class previously.

Multiplication:

$$3 \times 5 \stackrel{\text{def}}{=} 5 + 5 + 5 \rightarrow \text{means by definition}$$

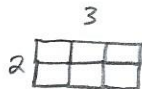
Definition -

In general, if m and n are whole numbers,

$$m \times n = \begin{cases} \overbrace{n+n+\dots+n}^m, & \text{if } m \neq 0 \\ 0, & \text{if } m = 0 \end{cases}$$

Ex.

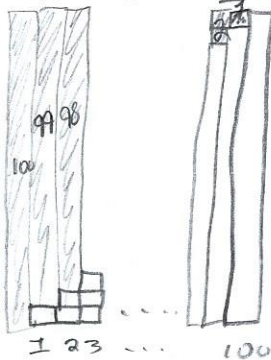
$$2 \times 3 = 3 + 3$$



$$3 \times 2 = 2 + 2 + 2$$



Sum of 1 to 100 integers:



100 boxes tall

So,

$$\frac{100 \times 101}{2}$$

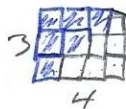
\rightarrow b/c we copied the boxes twice.

$$\frac{n(n+1)}{2}$$

generalized to any n whole #'s!

Ex.

$$1 + 2 + 3$$



\Rightarrow Number of blocks?

$$\frac{3 \cdot 4 = 12}{2 \cdot 2} = \boxed{6}$$

Powers of 10

• Notice that the number of numbers in any number grid is a 1 followed by some zeros.

• There are 10 1-digit numbers

• There are 100 2-digit numbers (incl. 00, 01, 02, ... etc)

$$\begin{aligned}100 &= 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 \\ &= 10 \times 10\end{aligned}$$

$$\begin{aligned}1000 &= 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 \\ &= 10 \times 100 \\ &= 10 \times \overbrace{10 \times 10} \\ &= 10^3\end{aligned}$$

In general,

$$10^{n+1} = 10 \times 10^n$$

10^n is a 1 followed by n zeros.

It can be useful to write numbers using powers of ten like so:

$$\begin{aligned}1,234 &= 1,000 + 200 + 30 + 4 \\ &= (1000) + (100+100) + (10+10+10) + 4 \\ &= 1 \times 1000 + 2 \times 100 + 3 \times 10 + 4 \\ &= 1 \times 10^3 + 2 \times 10^2 + 3 \times 10^1 + 4 \times \underline{10^0} \rightarrow 1\end{aligned}$$

— Expanded Form —