

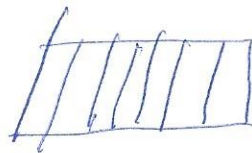
9/11/18

\* Describing the shape of histograms:

Symmetric distributions: If we split our histogram the left and right sides look like mirror images.

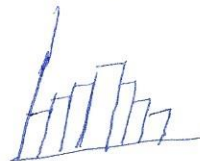
- uniform distributions:

\* classes with same frequency or relative frequency.



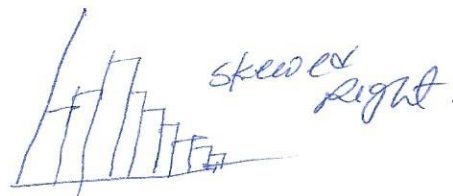
- bell-shaped distributions:

Highest frequency occurs in the middle and the frequencies fall off evenly on both sides.



bell shaped.

skewed right: longer tail to the right of the peak.



skewed right.

Skewed left: longer tail to the left of the peak.



skewed left.

\* Measures of Central Tendency

Mean  
Median  
mode

\* population mean (parameter)

if  $x_1, \dots, x_n$  are the  $N$  observations of a variable from a population. Then the population mean is

$$\mu = \frac{x_1 + x_2 + \dots + x_n}{N} = \frac{\sum x_i}{N}$$

\* sample mean (statistic)

if  $x_1, x_2, \dots, x_n$  are the  $n$  observations of a variable from a sample, then the sample mean is

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{\sum x_i}{n}$$

Example 1: (a)  $\mu = \frac{32 + 77 + 90 + 71 + 62 + 68 + 74 + 84 + 94 + 88}{10}$   
 $= \frac{790}{10} = \boxed{79}$

(b)  $\bar{x} = \frac{62 + 88 + 77 + 68}{4}$   
 $= \frac{295}{4} = \boxed{73.75}$

Median

Step 1: Arrange data in ascending order.

Step 2: Determine the number of observations,  $n$ .

Step 3: Determine the observations in the middle of the data set.

if  $n$  is odd the median is the data value in  $\frac{n+1}{2}$  position.

if  $n$  is even, the median is the average of the data values in position  $\frac{n}{2}$  and  $\frac{n}{2} + 1$ .

~~Mean~~: A numerical summary is said to be resistant if extreme values (very large or very small) relative to the data set do not affect its value substantially.

Mean is not resistant

Median is resistant.

Mode: value that occurs the highest number of times.

No mode, occurs when no observations appear more than once.

one mode, occurs when one observation appears more than the others.

two modes - if a data set has two modes we call it 'bimodal'.

More than two modes - Multimodal.