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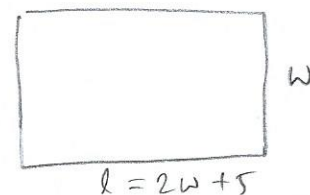
$$\begin{aligned} & \frac{8x}{x^2-9x+18} \div \frac{x^2+4x}{x^2-9} \cdot \frac{x-6}{x+3} \\ &= \frac{8x}{x^2-9x+18} \cdot \frac{x^2-9}{x^2+4x} \cdot \frac{x-6}{x+3} \\ &= \frac{8x}{(x-6)(x-3)} \cdot \frac{(x+3)(x-3)}{x(x+4)} \cdot \frac{(x-6)}{(x+3)} \\ &= \frac{8}{x+4} \end{aligned}$$

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$$\begin{aligned} & \frac{3x}{x^2+x-20} \cdot \frac{x^2-16}{x^2+9x} \div \frac{x+4}{x+9} \\ &= \frac{3x}{(x+5)(x-4)} \cdot \frac{(x+4)(x-4)}{x(x+9)} \cdot \frac{(x+9)}{(x+4)} \\ &= \frac{3}{x+5} \end{aligned}$$

The length of a rectangle is 5m more than double the width, and the area of the rectangle is 63 m^2 . Find the dimensions of the rectangle.

let. $l = \text{length}$ $l = 2w + 5$
 $w = \text{width}$



$$lw = 63$$

$$w(2w + 5) = 63$$

$$2w^2 + 5w = 63$$

$$2w^2 + 5w - 63 = 0$$

$$(2w - 9)(w + 7) = 0$$

$$2w - 9 = 0 \quad \text{OR} \quad w + 7 = 0$$

$$w = 9/2 \quad \quad \quad w = -7$$

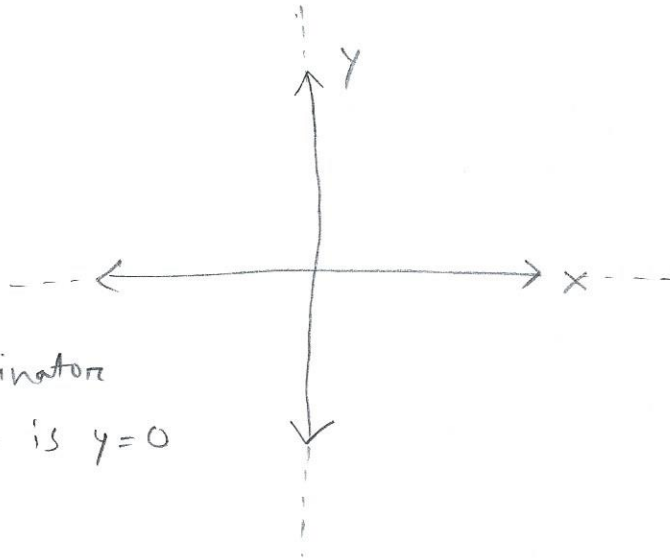
$$w = 4.5 \text{ m}$$

$$l = 2\left(\frac{9}{2}\right) + 5$$
$$= 14 \text{ m}$$

$f(x) = \frac{1}{x}$

$$x \neq 0$$

if the degree of the numerator is less than the degree of the denominator the horizontal asymptote is $y = 0$



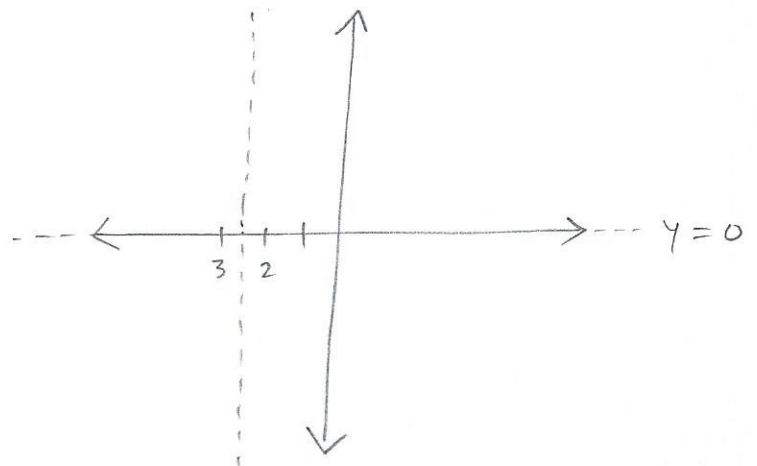
$$f(x) = \frac{-3}{-4x - 10}$$

vertical asymptote $x = -2.5$

$$-4x - 10 \neq 0$$

$$\frac{-4x}{-4} \neq \frac{10}{-4}$$

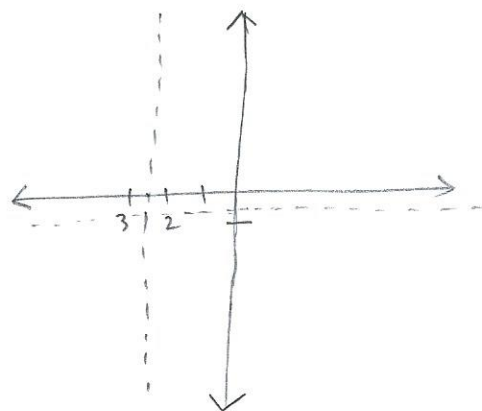
$$x \neq -\frac{5}{2}$$



if the degree of the numerator & denominator are the same, divide the leading coefficients to find the horizontal asymptote.

$f(x) = \frac{2x+5}{-4x-10}$ vertical asymptote $x = -2.5$

horizontal asymptote $y = -\frac{2}{4}$
 $y = -\frac{1}{2}$



if the degree of the numerator is greater than the degree of the denominator, there are no horizontal asymptotes.

$f(x) = \frac{2x^2+5}{-4x-10}$

Review :

Exponent Rules

1) $(2x^3y^2)(5x^2y) = 10x^5y^3$

2) $\frac{r^2}{2r^3} = \frac{1}{2r}$

3) $\frac{x^{-5}}{x^{-3}} = \frac{x^3}{x^5} = x^{-2} = \frac{1}{x^2}$

4) $(3m^2)^{-2} = 3^{-2}m^{-4} = \frac{1}{3^2m^4} = \frac{1}{9m^4}$

5) $\frac{4x^0y^{-2}z^3}{4x} = \frac{z^3}{xy^2}$

$$6) \left(\frac{3}{5}\right)^{-3} = \left(\frac{5}{3}\right)^3 = \frac{5^3}{3^3} = \frac{125}{27}$$

Polynomial long division

$$7) (4x^2 + 14x + 12) \div (2x + 4) = 2x + 3$$

$$\begin{array}{r}
 2x+3 \\
 \hline
 2x+4 \overline{) 4x^2+14x+12} \\
 \underline{4x^2+8x} \\
 6x+12 \\
 \underline{6x+12} \\
 0
 \end{array}$$

Polynomial long division OR synthetic division

$$8) (x^2 + 5x + 4) \div (x + 2)$$

$$= x + 3 + \frac{-2}{x+2}$$

$$\begin{array}{r|rrr}
 & 1 & 5 & 4 \\
 -2 & \downarrow & -2 & -6 \\
 \hline
 & 1 & 3 & -2
 \end{array}$$

Simplifying Rational expressions

$$9) \frac{-70n^2}{28n^5} = \frac{-5}{2n^3}$$

$$10) \frac{x+6}{x^2+5x-6} = \frac{(x+6)}{(x+6)(x-1)} = \frac{1}{x-1}$$

$$11) \frac{3x^2 - 39x + 90}{x^2 - 3x - 70} = \frac{3(x^2 - 13x + 30)}{x^2 - 3x - 70} = \frac{3(x-3)(x-10)}{(x-10)(x+7)} = \frac{3(x-3)}{x+7}$$

$$\begin{aligned}
 12) \frac{2x}{x^2+5x-6} \div \frac{x^2-3x}{x^2-36} \cdot \frac{x-3}{x-6} \\
 = \frac{2\cancel{x}}{(x+6)(x-1)} \cdot \frac{(x+6)(x-6)}{\cancel{x}(x-3)} \cdot \frac{(x-3)}{(x-6)} \\
 = \frac{2}{x-1}
 \end{aligned}$$